

# Ambiguous Grammars

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## Definitions

- If a grammar has more than one leftmost derivation for a single *sentential form*, the grammar is *ambiguous*
- If a grammar has more than one rightmost derivation for a single sentential form, the grammar is *ambiguous*
- The leftmost and rightmost derivations for a sentential form may differ, even in an unambiguous grammar
  - However, they must have the same parse tree!

Classic example — the *if-then-else* problem

$$\begin{array}{l} Stmt \rightarrow \underline{if} \ Expr \ \underline{then} \ Stmt \\ \quad \quad | \ \underline{if} \ Expr \ \underline{then} \ Stmt \ \underline{else} \ Stmt \\ \quad \quad | \ \dots \ other \ stmts \ \dots \end{array}$$

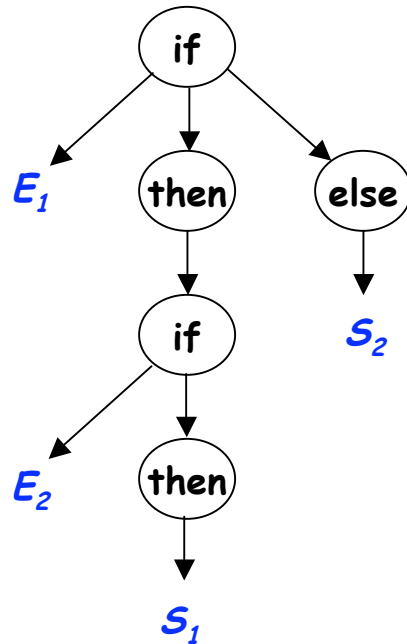
*This ambiguity is entirely grammatical in nature*

# Ambiguity

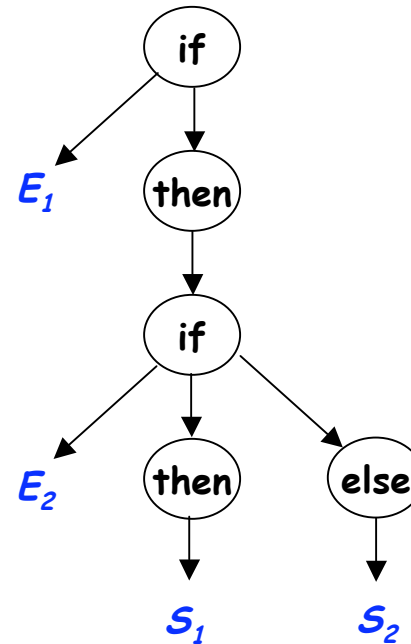


This sentential form has two derivations

if  $Expr_1$  then if  $Expr_2$  then  $Stmt_1$  else  $Stmt_2$



*production 2,  
then production 1*



*production 1,  
then production 2*

# Ambiguity



## Removing the ambiguity

- Must rewrite the grammar to avoid generating the problem
- Match each else to innermost unmatched if (*common sense rule*)

1		<i>Stmt</i>	→	<u>if</u> <i>Expr</i> <u>then</u> <i>Stmt</i>
2				<u>if</u> <i>Expr</i> <u>then</u> <i>WithElse</i> <u>else</u> <i>Stmt</i>
3				<i>Other Statements</i>
4		<i>WithElse</i>	→	<u>if</u> <i>Expr</i> <u>then</u> <i>WithElse</i> <u>else</u> <i>WithElse</i>
5				<i>Other Statements</i>

With this grammar, example has only one rightmost derivation

Intuition: once into *WithElse*, we cannot generate an unmatched else  
... a final if without an else can only come through rule 2 ...

# Ambiguity



if  $Expr_1$  then if  $Expr_2$  then  $Stmt_1$  else  $Stmt_2$

Rule	Sentential Form
—	$Stmt$
1	<u>if</u> $Expr$ <u>then</u> $Stmt$
2	<u>if</u> $Expr$ <u>then</u> <u>if</u> $Expr$ <u>then</u> $WithElse$ <u>else</u> $Stmt$
3	<u>if</u> $Expr$ <u>then</u> <u>if</u> $Expr$ <u>then</u> $WithElse$ <u>else</u> $S_2$
5	<u>if</u> $Expr$ <u>then</u> <u>if</u> $Expr$ <u>then</u> $S_1$ <u>else</u> $S_2$
?	<u>if</u> $Expr$ <u>then</u> <u>if</u> $E_2$ <u>then</u> $S_1$ <u>else</u> $S_2$
?	<u>if</u> $E_1$ <u>then</u> <u>if</u> $E_2$ <u>then</u> $S_1$ <u>else</u> $S_2$



some other production

This grammar has only one rightmost derivation for the example